## Q-factor essentials sheet

Q-factor is a measure of 'quality' of a particular resonance. Each normal mode, ie mode of oscillation, of a system has two important things: its resonant frequency (sometimes called  $f_0$ ), and its Q-factor.

Q is a way of saying many things all at once, all of which follow from each other:

- high Q = 'high quality' = rings for many cycles (long decay time) after being hit
- = very little damping = peak width of frequency response is narrow
- = peak width of frequency response is tall.

Now in more detail... There are 2 simple things you can do to a system: hit it once (shown on left side) or excite (drive) it at a given frequency and see how much it responds (shown on right side) ...

## DECAY AFTER SINGLE HIT



Oscillation with exponential decay in time.  $\tau = how \ long \ to \ die \ to \ 1/e, \ about \ 37\%$ happens to be the definition  $Q = \pi \ times \ how \ many \ cycles \ in \ a \ decay \ time$   $= \pi \ (\tau / T)$   $= \pi f_0 \tau$   $= \omega_0 \tau / 2$  $using \ 1/T = f = \omega / 2\pi$ 

## RESPONSE TO DRIVING AT GIVEN FREQ



Low frequency response called C: all we're saying is the peak height is Q times this.

The peak width is *Q* times narrower than the position of the peak in frequency.

Eg tuning fork has many thousands of cycles during decay time -> high Q, whereas a piece of jello (jelly) only wobbles a few times before settling down -> low Q. Therefore if you want to excite the jello you don't have to get the driving frequency very accurate; with tuning fork you do.

It is amazing that all these properties are controlled through a single quantity, Q.