

## Arm Cavity g-factorを本当にどうするべきか?

- ビームサイズ: 本当に広げる必要があるか?
- PIをg-factorの決め手にするべきではない?(by reviewers)
- Sidles-Sigg: やはりNegative g-factorが良いようにも思える。。。
- 鏡研磨の精度がわからない。。。

# Cavity g-factor

## Relevant Issues

- Beam spot size --> Mirror Thermal Noise
- Angular radiation pressure (Sidles-Sigg Instability)
- Parametric Instability

### Proposed g-factors from Detector Configuration Group

$g_1 = 0.87, g_2 = 0.6 \rightarrow R_1 = \underline{23\text{km}}, R_2 = 7.7\text{km}$

or

$g_1 = -0.87, g_2 = -0.6 \rightarrow R_1 = 1.6\text{km}, R_2 = 1.9\text{km}$

Possible ?

### Old g-factors

$g_1 = g_2 = 0.586 \rightarrow R_1 = R_2 = 7.2\text{km}$

or

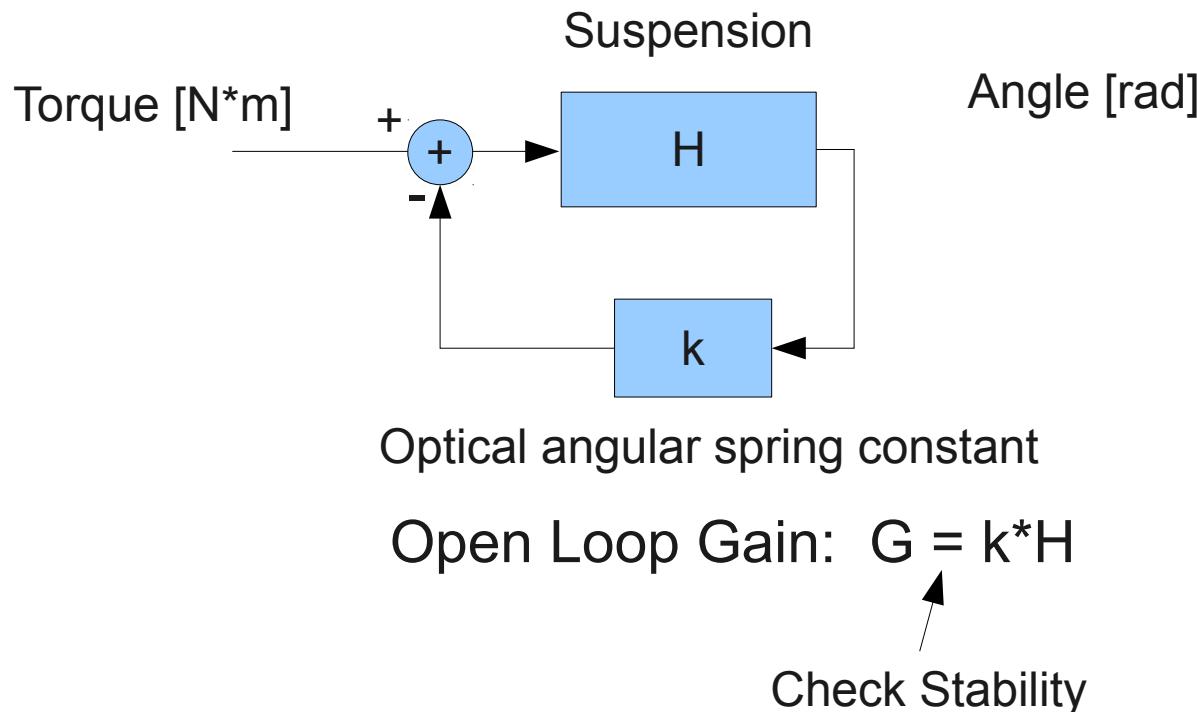
$g_1 = g_2 = -0.586 \rightarrow R_1 = R_2 = 1.9\text{km}$

# Sidles-Sigg Stiffness Matrix

Angular Optical Spring Constant  $k$  [N\*m/rad]

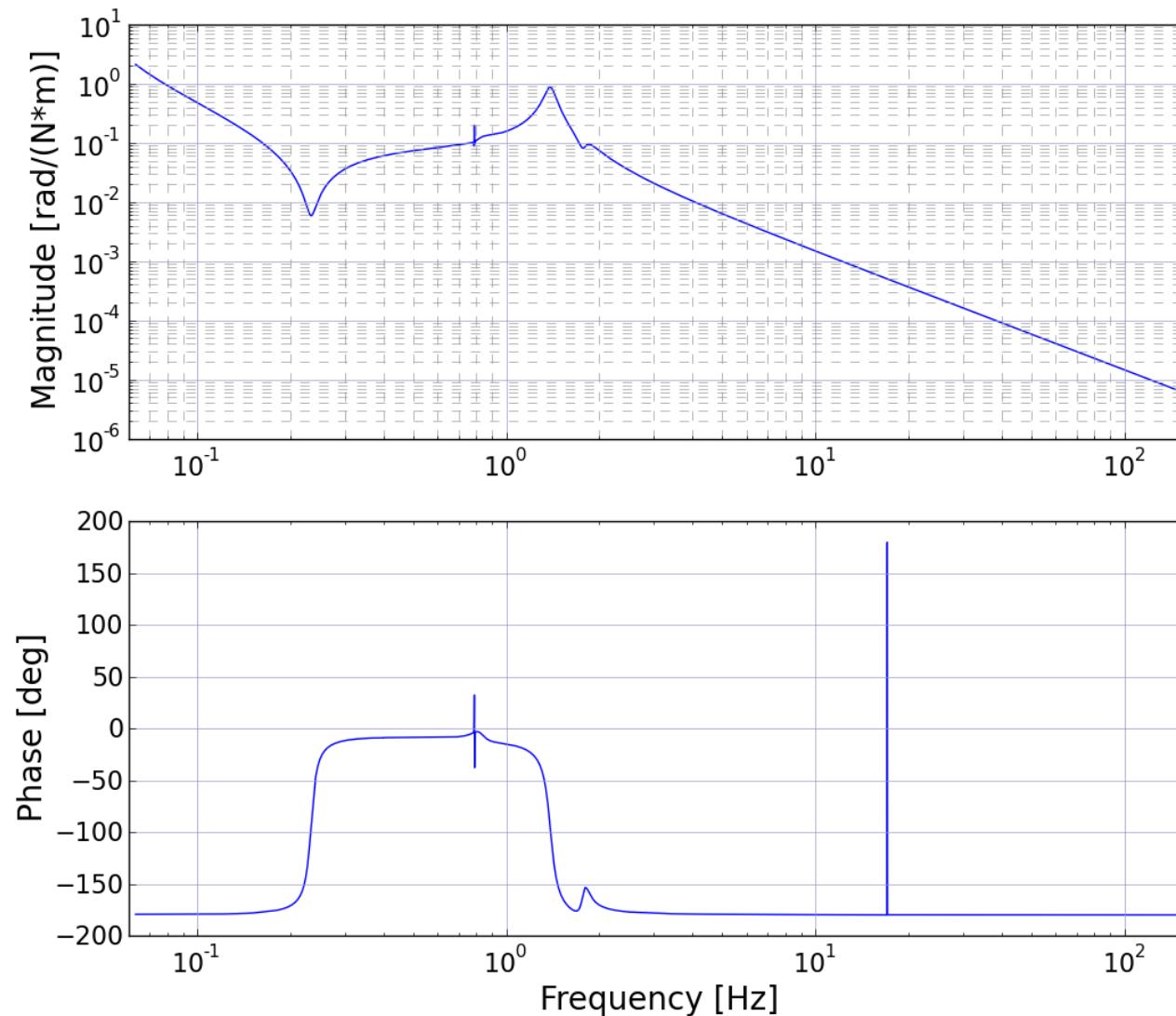
New g-factors  
4.59, -29.2 ( $g_1 = 0.87$ ,  $g_2 = 0.6$ )  
-4.59, 29.2 ( $g_1 = -0.87$ ,  $g_2 = -0.6$ )

Old g-factors  
5.0, -19.33 ( $g_1 = g_2 = 0.586$ )  
-5.0, 19.33 ( $g_1 = g_2 = -0.586$ )



# Suspension TF (by Sekiguchi-kun)

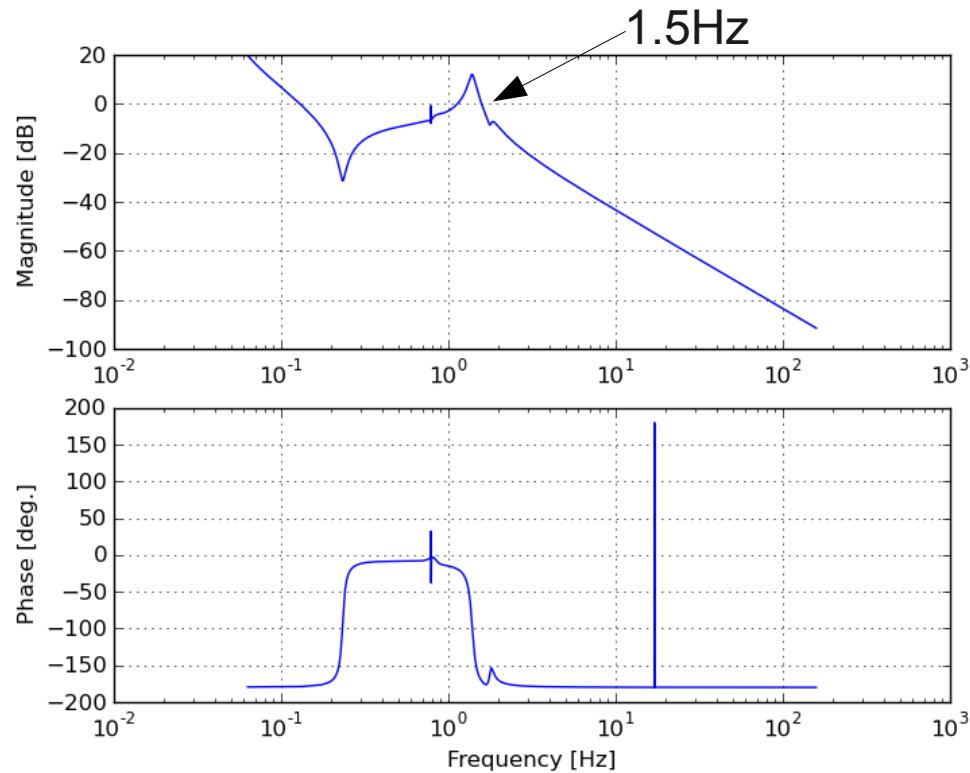
Yaw Torque -> Yaw Angle



This is H

## Open Loop TF

New g-factor, positive



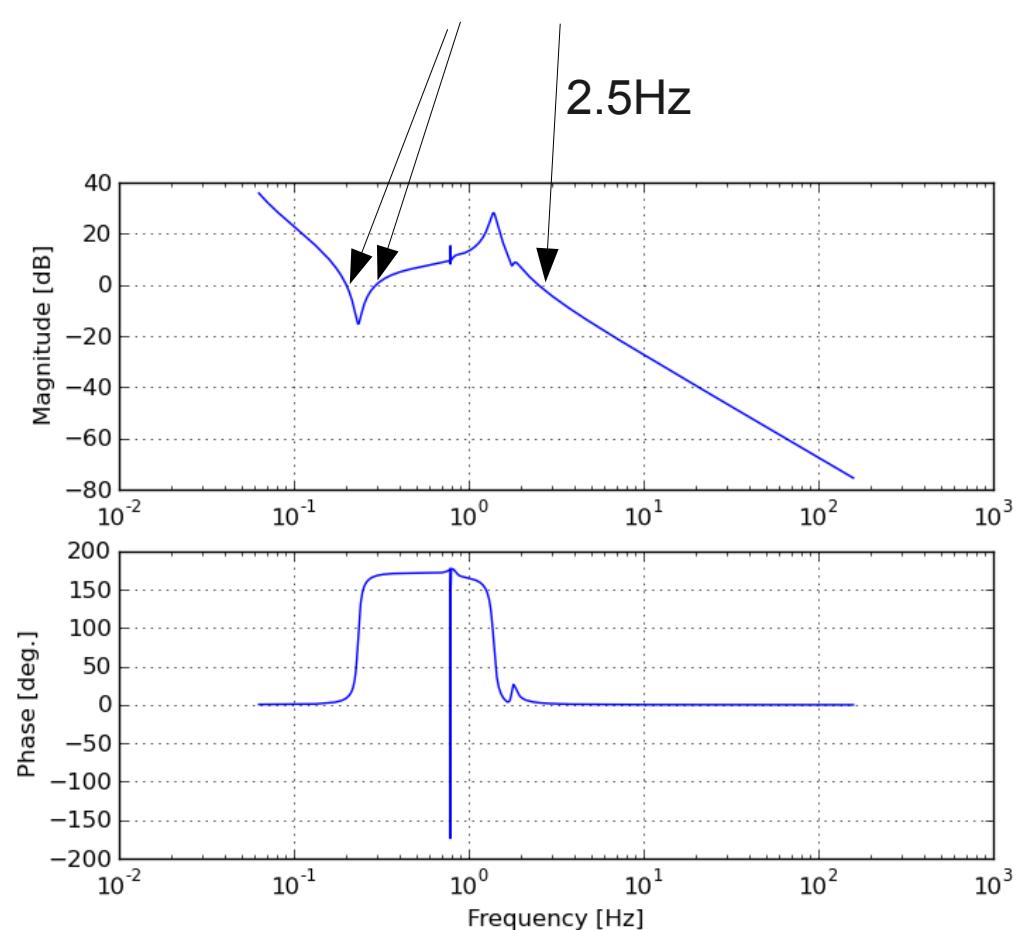
Stable

Unstable

2.5Hz

Unstable frequency

Positive g-factor: 2.5Hz  
Negative g-factor: 1.5Hz



## Open Loop TF

Old g-factor, positive

Stable

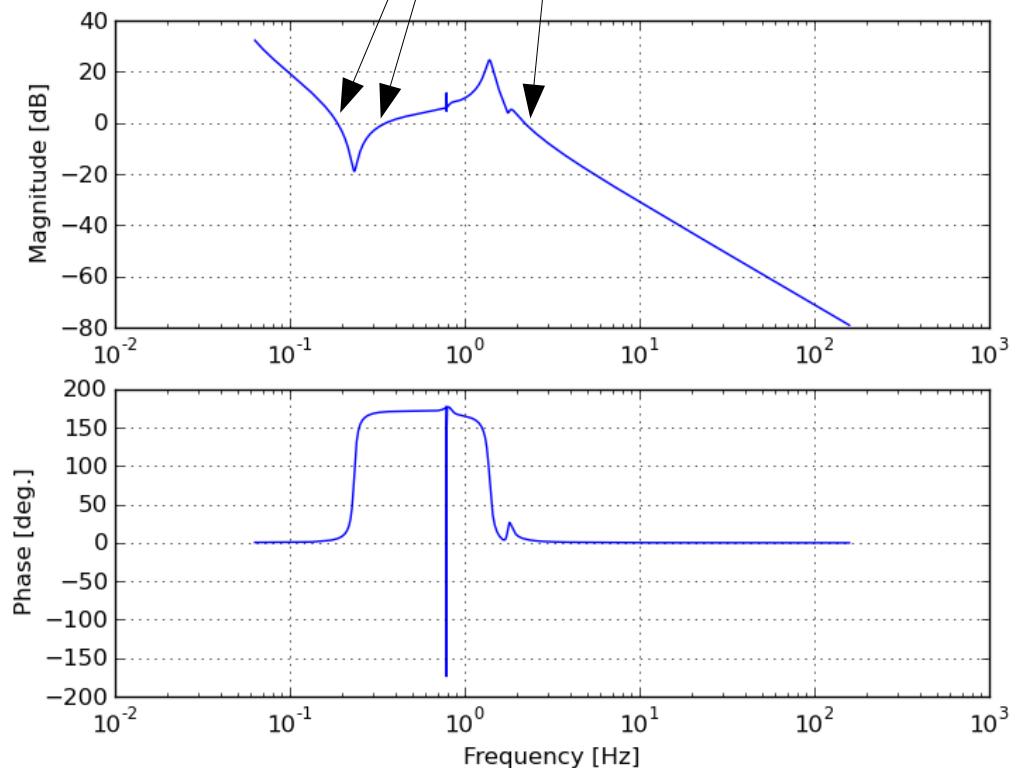
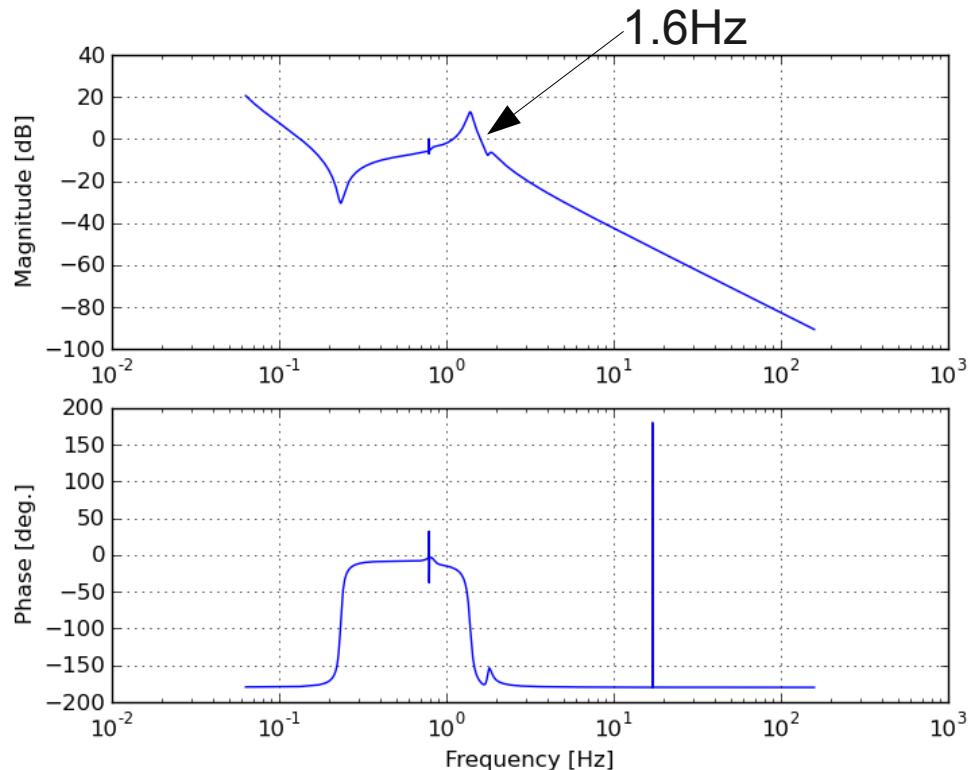
Unstable

2.2Hz

Unstable frequency

Positive g-factor: 2.2Hz  
Negative g-factor: 1.6Hz

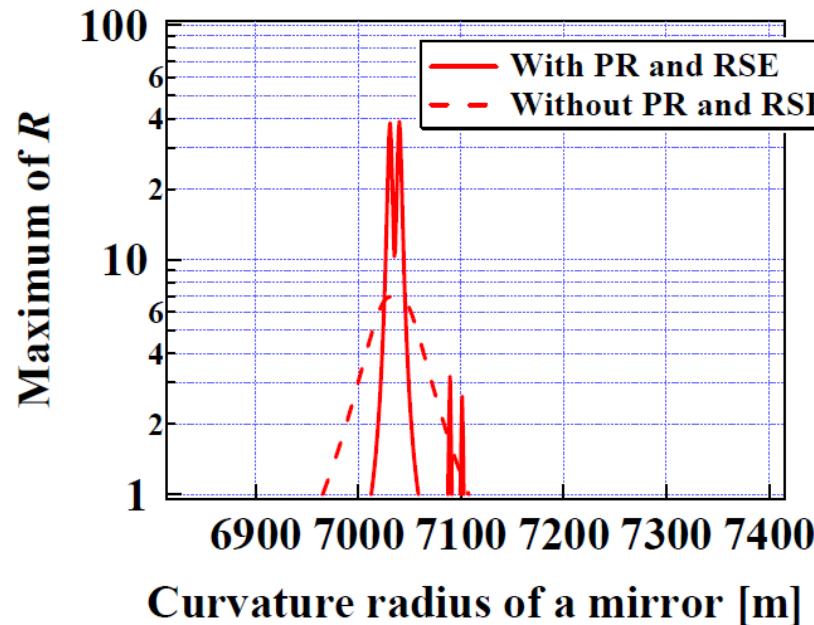
No big difference in terms of  
the Sidles-Sigg instability



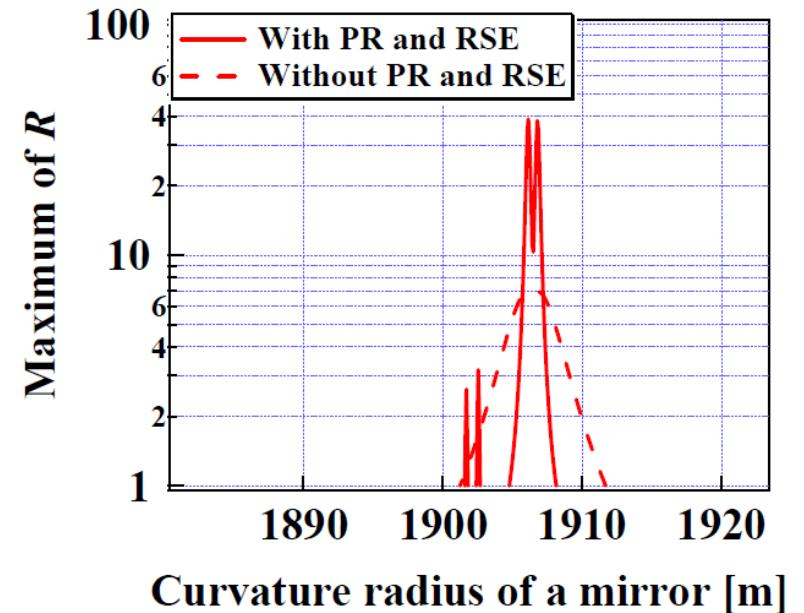
# Parametric Instability

There are dangerous regions to avoid in the g-factor space

Positive g-factor



Negative g-factor



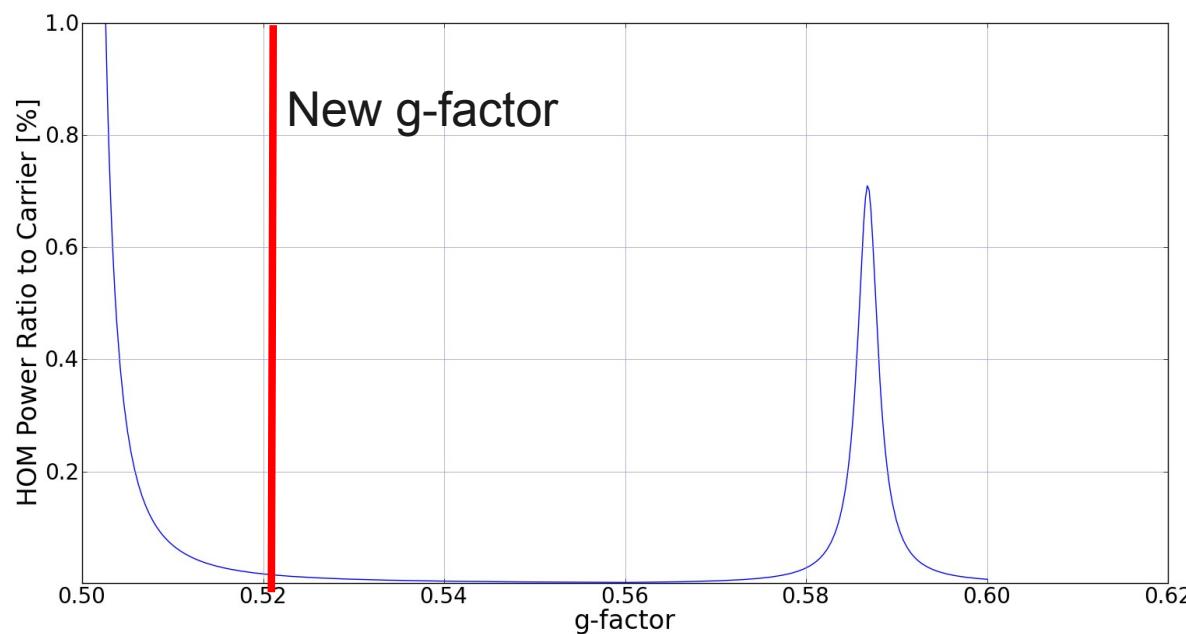
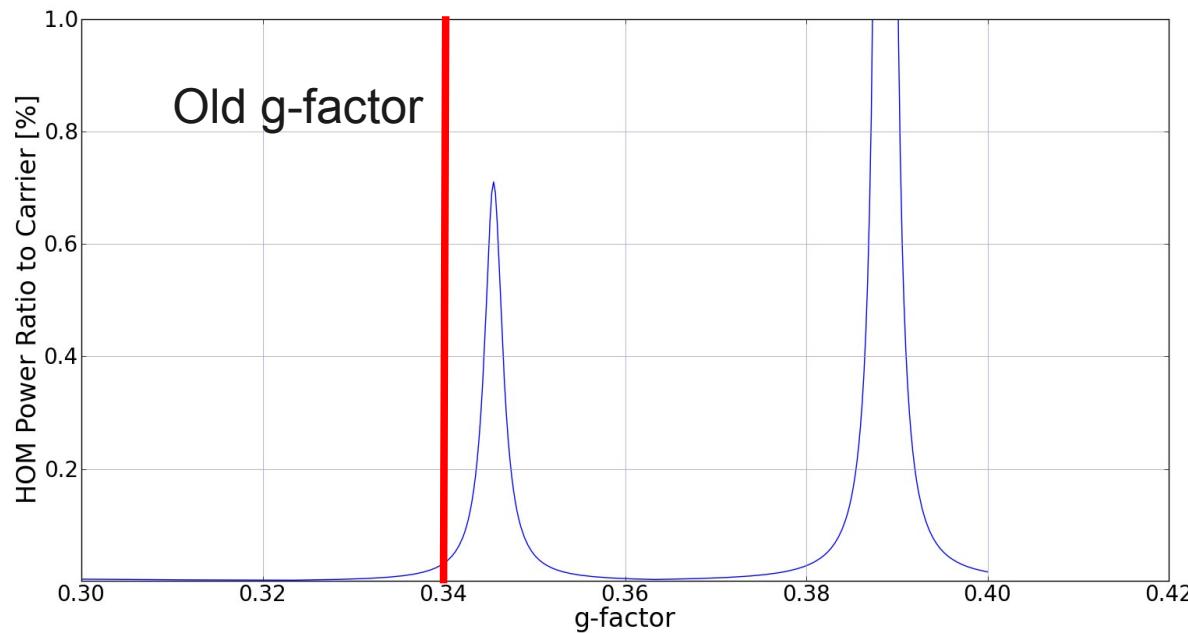
The error requirement on the mirror ROC is stricter for the negative g-factor.  
by  $(R_p/R_n)$

Negative g-factor:  $R \sim 1.9\text{km}$   
Positive g-factor:  $R > 7\text{km}$

Negative g-factor is about 3.7 times more  
severe to ROC error in terms of PI

10m ROC error for 1.9km mirror -> 0.5% error  
100m ROC error for 7km mirror -> 1.5% error

# Max HOM Resonances in the arm



# Conclusion on g-factor

Please vote !

		Thermal Noise (IR) DRSE/BRSE [Mpc]	Optical Spring Unstable Freq.	PI	Other
(a)	$g_1=0.87$ $g_2=0.6$	273/245	2.5Hz	Easy	ROC=23km may not be possible
(b)	$g_1=-0.87$ $g_2=-0.6$	273/245	1.5Hz	Severe	
(c)	$g_1=0.586$ $g_2=0.586$	266/241	2.2Hz	Easy	iLIGO mirrors can be used.
(d)	$g_1=-0.586$ $g_2=-0.586$	266/241	1.6Hz	Severe	

## 三尾先生のコメント

超長曲率半径鏡の件、問い合わせをしていますが、回答がありません。フラットだとダメなんですか？0.5%の話は一応、会社に伝えてありますが、測れないというのが現状でしょう。

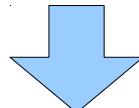
どっちにしろ、測定ができれば、磨けると思います。たぶん。

どっちが難しいかというのは、あまりいい質問のように思えません。どっちも難しいということになりそう。

ごめん、あんまり、きちんと対応できる時間と頭がありません。

23kmミラー -> 出来るかどうか不透明

0.5%エラー -> 出来るかどうか不透明



現状で選択できるのは(c)しかない？